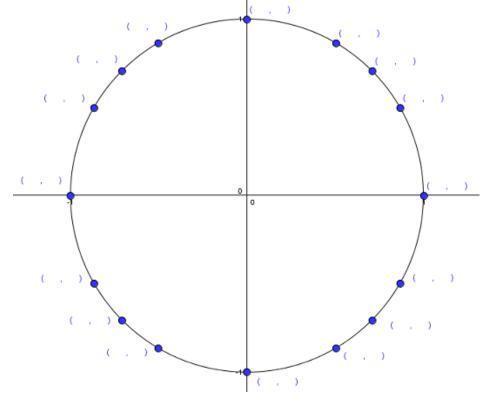
Name: \_\_\_\_\_

## SM3 6.3 Evaluate Six Trig Functions

<u>Vocab/Def</u> :	Name of function Sine	SM2 Definition $\sin \theta = \frac{opp}{hyp}$	& Algebraic Manipulation	Knowledge needed for success in SM3 $\sin\theta$ is the $y$ -value on the unit circle
	Cosine	$\cos\theta = \frac{adj}{hyp}$		$\cos \theta$ is the $x$ -value on the unit circle
	Tangent	$\tan\theta = \frac{opp}{adj}$	/ hyp	$\tan \theta = \frac{\sin \theta}{\cos \theta}$
	Cotangent	$\cot \theta = \frac{adj}{opp}$	/ II V I)	$\cot \theta = \frac{\cos \theta}{\sin \theta}$
	Secant	$\sec \theta = \frac{hyp}{adj}$	$=\frac{1}{adj/hyp} = \frac{1}{\cos\theta}$	$\sec \theta = \frac{1}{\cos \theta}$
	Cosecant	$\csc\theta = \frac{hyp}{opp}$	$=\frac{1}{opp/hyp} = \frac{1}{\sin\theta}$	$\csc\theta = \frac{1}{\sin\theta}$

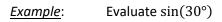
*Label*: Place the x and y coordinate values on the unit circle:,



It is more important for you to be able to quickly navigate about the unit circle than to memorize each location.

Look for patterns so you can leap from position to position quickly!

 $\sin\theta$  is defined as  $\frac{opp}{hyp}$  in a right triangle. Since hyp=1,  $\sin\theta=opp$ , which is the y-value on the unit circle.



The *y*-value on the unit circle in the 30° is  $\frac{1}{2}$ 

$$\sin(30^\circ) = \frac{1}{2}$$

## **Example**: Evaluate sec(30°)

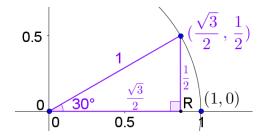
$$\sec(30^\circ) = \frac{1}{\cos(30^\circ)} = \frac{1}{\sqrt{3}/2} = \frac{2}{\sqrt{3}} = \frac{2\sqrt{3}}{3}$$

$$\sec(30^\circ) = \frac{2\sqrt{3}}{3}$$

## **Example**: Evaluate tan(30°)

$$\tan(30^\circ) = \frac{\sin(30^\circ)}{\cos(30^\circ)} = \frac{1/2}{\sqrt{3}/2} = \frac{1}{\sqrt{3}} = \frac{\sqrt{3}}{3}$$

$$\tan(30^\circ) = \frac{\sqrt{3}}{3}$$



<u>Problems</u>: Evaluate the trigonometric expressions of degree measurements:

1) 
$$\sin(45^{\circ})$$
 2)  $\cos(45^{\circ})$  3)  $\sec(45^{\circ})$  4)  $\csc(45^{\circ})$  5)  $\tan(45^{\circ})$  6)  $\cot(45^{\circ})$ 

7) 
$$\sin(120^\circ)$$
 8)  $\cos(120^\circ)$  9)  $\sec(120^\circ)$  10)  $\csc(120^\circ)$  11)  $\tan(120^\circ)$  12)  $\cot(120^\circ)$ 

13) 
$$\sin(90^{\circ})$$
 14)  $\cos(90^{\circ})$  15)  $\sec(90^{\circ})$  16)  $\csc(90^{\circ})$  17)  $\tan(90^{\circ})$  18)  $\cot(90^{\circ})$ 

19) 
$$\sin(225^{\circ})$$
 20)  $\cos(135^{\circ})$  21)  $\sec(300^{\circ})$  22)  $\csc(120^{\circ})$  23)  $\tan(240^{\circ})$  24)  $\cot(330^{\circ})$ 

25) 
$$\sin(450^{\circ})$$
 26)  $\cos(-90^{\circ})$  27)  $\sec(-30^{\circ})$  28)  $\csc(600^{\circ})$  29)  $\tan 150^{\circ}$  30)  $\cot(750^{\circ})$ 

Evaluate the trigonometric expressions of radian measurements:

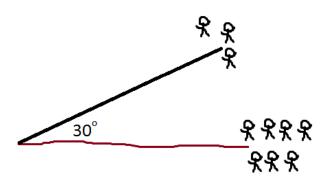
31) 
$$\sin\left(\frac{\pi}{6}\right)$$
 32)  $\cos\left(\frac{\pi}{6}\right)$  33)  $\sec\left(\frac{\pi}{6}\right)$  34)  $\csc\left(\frac{\pi}{6}\right)$  35)  $\tan\left(\frac{\pi}{6}\right)$  36)  $\cot\left(\frac{\pi}{6}\right)$ 

$$\sin\left(\frac{2\pi}{3}\right) \quad 38) \quad \cos\left(\frac{4\pi}{3}\right) \quad 39) \quad \sec\left(\frac{3\pi}{4}\right) \quad 40) \quad \csc\left(\frac{7\pi}{6}\right) \quad 41) \quad \tan\left(\frac{11\pi}{6}\right) \quad 42) \quad \cot\left(\frac{5\pi}{4}\right) \quad 43) \quad 43)$$

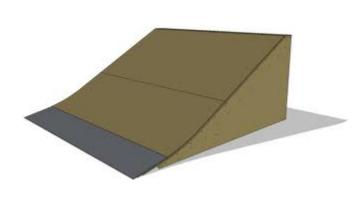
43) 
$$\sin(\pi)$$
 44)  $\cos(\frac{\pi}{2})$  45)  $\sec(\frac{\pi}{2})$  46)  $\csc(\frac{\pi}{2})$  47)  $\tan(\frac{\pi}{2})$  48)  $\cot(\pi)$ 

49) 
$$\sin\left(\frac{13\pi}{6}\right)$$
 50)  $\cos\left(-\frac{14\pi}{3}\right)$  51)  $\sec\left(\frac{61\pi}{6}\right)$  52)  $\csc\left(-\frac{5\pi}{6}\right)$  53)  $\tan\left(-\frac{31\pi}{6}\right)$  54)  $\cot\left(\frac{17\pi}{2}\right)$ 

A secondary math 3 class takes a hiking trip and walks due east into along a trail. Nate, Mitch, and Lincoln fail to pay enough attention to the trail and begin to deviate from the proper course by 30 degrees north of east. After an hour, the class has hiked one mile.



- 55) Are the wayward students directly north of the main group of students?
- 56) Why or why not?
- 57) About how far north of the trail are the wayward students?



Beth purchases a skate board ramp with a cool innovation: adjustable angle of elevation. The ramp has a ramp length of 1 meter.

- 58) Not wanting to break her legs on the first approach, Beth sets her ramp's angle of elevation to a mere 30°. How far off of the ground is Beth's skateboard when it leaves the ramp?
- 59) How high would the skateboard be if the ramp were set to  $45^{\circ}$ ?
- 60) How high would the skateboard be if the ramp were set to  $60^{\circ}$ ?
- 61) How high would the skateboard be if the ramp were set to  $90^{\circ}$ ?